

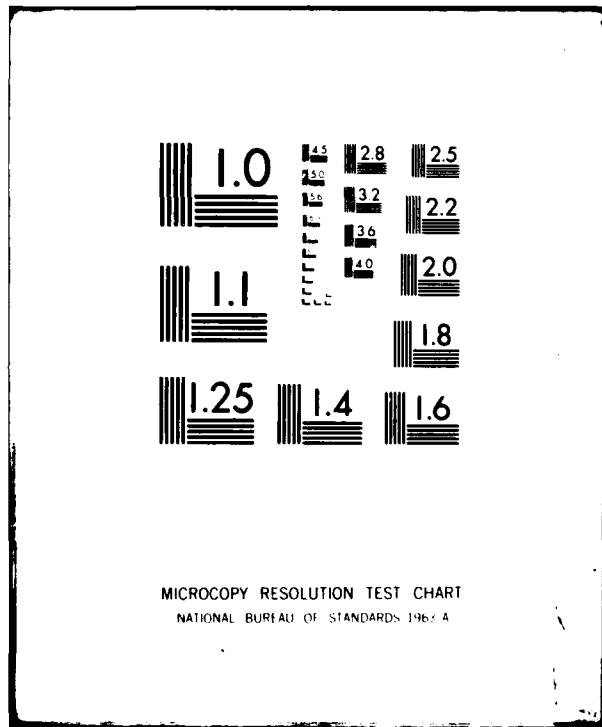
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SIMULTANEOUS OBSERVATIONS OF GLOBAL POSITIONING SYSTEM (GPS) SA--ETC(U)  
MAR 82 B R HERMANN, A G EVANS  
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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) Two conventional code tracking Global Positioning System (GPS) receiver systems were used to simultaneously track GPS satellites on a short baseline. Six-second pseudorange observations and range differences from 1-min Doppler counts at a single frequency were obtained from each receiver. Relative positioning of the receiver antennas was conducted over zero-length and 2-m baselines. Common and independent frequency standards were used on different days; the results were compared.		

## FOREWORD

The development of the NAVSTAR Geodetic Receiver System (NGRS) was funded by the Defense Mapping Agency as a means to demonstrate the capability of using the Global Positioning System (GPS) transmissions to achieve high-accuracy geodetic positioning. The receiver was designed by Stanford Telecommunications Incorporated. The supporting hardware and the system microprocessor controller software were proposed and implemented at the Naval Surface Weapons Center (NSWC) by the Advanced Projects Division, Electronics Systems Department. Data reduction was performed by the Space Flight Sciences Branch and the Physical Sciences Software Branch of the Space and Surface Systems Division, Strategic Systems Department. Technical and administrative assistance was received from the sponsor through the Defense Mapping Agency Hydrographic/Topographic Center, Washington, D.C.

Released by:

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## INTRODUCTION

NSWC has developed two Navstar Geodetic Receiver Systems (NGRSs) that utilize Stanford Telecommunication Inc. (STI) GPS receivers. The first NGRS was operational in February 1979, and data was gathered at several sites in the United States during that year. Throughout 1980, the first system was progressively modified so that it and the second system (developed in 1980) had as much common hardware and software as practical. The primary differences between the two systems are related to the differences in the two STI receivers employed: the first NGRS utilizes a STI model 5007 receiver, while NGRS-2 utilizes a model 5010. The later model 5010 has the capability of L<sub>1</sub> pseudorange observations and also provides dual-frequency 6-s digital Doppler count output, while the 5007 does not.

Each system, which is composed of the components listed in Table 1, is mounted in three 5-ft racks. The microprocessor software and the processing software that reads the recorded data tapes were developed at NSWC. A more detailed system description is given in Reference 1.

Table 1. NGRS Components

Microprocessor Controller	INTEL 80/10
Frequency Standard	HP 5061A-004
GPS Receiver	STI 5007 or STI 5010
GPS Test Transmitter	STI 5001A
Time-Interval Counters	HP 5370 and HP 5328
Full-Cycle Doppler Counter	NSWC
Digital Clock	HP 59309A
Antenna	CKU CA3207
Tape Recorder	KENNEDY 9800
Keyboard/Display	ADM-3
Power Buffer	ELGAR UPS 252-1

## **NGRS DATA DESCRIPTION**

The original intent of the NGRS was to utilize the pseudorange solely as a means to obtain the local clock correction. Since microsecond accuracy is adequate for that purpose, only single-frequency L<sub>1</sub> pseudorange capability with limited resolution was provided by NGRS-1.

The single-frequency pseudorange measurement was upgraded in NGRS-1 (1980) by replacing the 10-ns time-interval counter with a 20-ps counter. This improved the RMS noise level from 1.5 m (truncation limited) to 70 cm (receiver limited). NGRS-2, which utilizes the model 5010 receiver, has two 200-ps counters. In all cases, the observation is the time interval between the local 6-s epoch and the received epoch.

In order to obtain ionospheric corrected range difference observations, dual-frequency analog Doppler signals are used. Since these signals are analog, a counter external to the receiver is required. A 60-s nominal count interval was chosen. This method of providing continuous Doppler observations is used in both systems. At each local minute epoch, the current reading of the L<sub>1</sub> or L<sub>2</sub> Doppler counter is strobed and the time interval to the next positive zero crossing is measured. These two quantities are used to construct the cycle count during the previous 1-min interval. The range difference can then be computed using the two frequency observations<sup>1</sup>.

The time-of-arrival difference for signals emanating from a satellite and received at two stationary (in the earth fixed frame) sites can be used to determine the baseline connecting the two sites. The data class described is a range difference in space at a common time. The NGRS are primarily designed to obtain range differences in time at a fixed site; consequently, the Doppler count data cannot be used directly in the time-of-arrival difference problem. If the two sites are considered to be independent and do not communicate in real time, the most straightforward arrangement with the NGRS is to plan the observations so that the two receivers track the same satellites simultaneously and record pseudoranges and Doppler counts in the usual manner. When the data are later processed, the pseudoranges from each satellite-to-site combination can be computed, evaluated at a common time, and differenced to obtain the desired range difference between the sites. Both the pseudorange and Doppler data are processed together. However, since the Doppler carries no absolute range information, the evaluation of the smoothed range is determined primarily by the quality of the pseudorange obsevations. The single-frequency measurements are adequate for relative positioning if the sites are not far apart, since then both receivers will see substantially the same ionospheric and tropospheric refraction effects.

## **FORMULATION**

The first adjustment that must be made to the two data sets is to convert to a common time system. In this application, the broadcast ephemeris, the broadcast satellite clock corrections, and

the observed pseudoranges can be used to determine a set of polynomial coefficients that will convert local time to GPS time<sup>2</sup>.

The 6-s pseudoranges are too frequent and too noisy to be used individually, so a smoothing polynomial is employed that also incorporates the range difference data. Only L<sub>1</sub> data are used, because NGRS-1 lacks L<sub>2</sub> pseudorange and the baseline involved is very short. The ionospheric correction to the L<sub>1</sub> range difference (derived from the Doppler) is computed and applied twice to account for the difference in sign between phase (Doppler) and group (range) delays introduced by the ionosphere<sup>3</sup>. The time tags attached to the pseudoranges are the local times of reception of the satellite epoch, while the range differences are tagged at the local epoch. These differ by the amount of the pseudorange measurement.

The smoothing range polynomial is defined as follows:

$$r(t_k) = a_0 + \sum_{i=1}^4 a_i (t_k - t_o)^i \quad (1)$$

In the case of range difference, it is  $r(t_j) - r(t_{j-1})$ .

$$r(t_j) - r(t_{j-1}) = \sum_{i=1}^4 a_i [(t_j - t_o)^i - (t_{j-1} - t_o)^i] \quad (2)$$

These two observation equations are used together in one least squares solution to solve for the a<sub>i</sub>'s. In a typical 10-min fit, there are 100 pseudorange observations and 10 range difference observations. However, the range differences are more accurate and are weighted by a factor of 20 to 1 over the pseudoranges.

Similar 10-min data spans from each site are smoothed and the resulting coefficients are used in Equation 1 to compute a range at a time near the middle of the span. The ranges are then differenced to obtain the equivalent time-of-arrival difference of the satellite signal at the two sites. Instead of fitting first and then differencing, the data might have been differenced first and then fitted. This has the following advantages: allows the use of a lower-order polynomial, introduces less numerical error, and utilizes a single fit rather than two fits. However, because the local clocks were not necessarily synchronized, the data were not obtained simultaneously; consequently, this option was abandoned.

The geometry of the relative positioning problem is illustrated in Figure 1. The pertinent vectors are defined below.

$t_T$	time of transmission
$t_R$	time of reception
$\bar{r}_s(t_T) = x_s \hat{x} + y_s \hat{y} + z_s \hat{z}$	satellite position
$\bar{r}_g(t_R) = x_g \hat{x} + y_g \hat{y} + z_g \hat{z}$	reference site position
$\bar{r}_h(t_R) = x_h \hat{x} + y_h \hat{y} + z_h \hat{z}$	secondary site position
$\bar{b}(t_R) = \bar{r}_h(t_R) - \bar{r}_g(t_R)$	baseline vector
$r =  \bar{r}_s(t_T) - \bar{r}_g(t_R) $	slant range, reference site
$r + \ell =  \bar{r}_s(t_T) - \bar{r}_h(t_R) $	slant range, secondary site

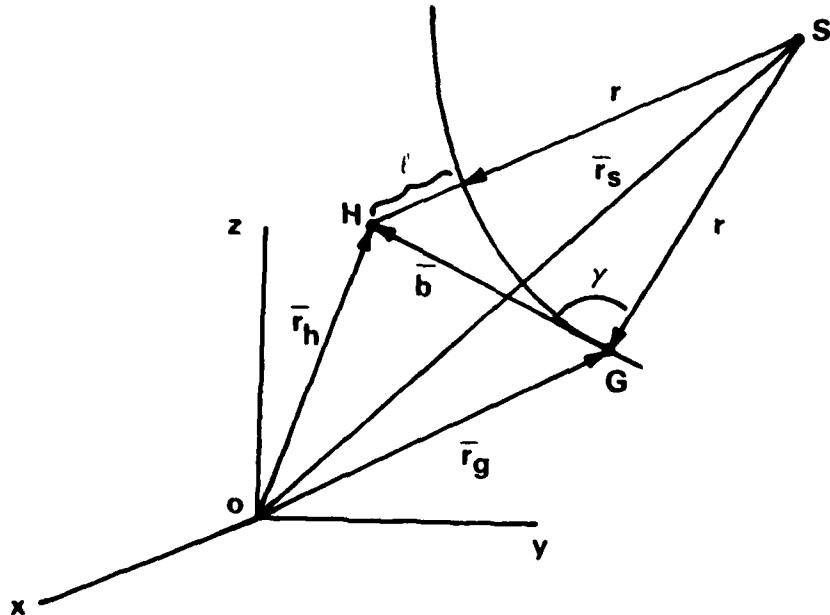


Figure 1. Simultaneous Observations of a Satellite From Two Sites

The  $x$ ,  $y$ ,  $z$  coordinate system in Figure 1 is an earth fixed frame; therefore, the vectors  $\bar{r}_g$ ,  $\bar{r}_h$ , and  $\bar{b}$  are independent of time. The satellite vector  $\bar{r}_s(t_T)$  is the only time-variable parameter. The differences in range from the satellite to the two sites is represented by  $\ell$  and is part of the observation obtained from differencing the two smoothing polynomials. The remaining portion of the observation is due to differences in receiver biases and will be represented by  $\ell_1 + \ell_2(t_R - t_o)$ . Thus, the observation equation is

$$L(\bar{r}_R) = \ell + \ell_1 + \ell_2(t_R - t_o) \quad (3)$$

The geometric part,  $\ell$ , is a function of the unknown baseline vector  $\bar{b}$ . In the triangle GHS,

$$(r + \ell)^2 = r^2 + b^2 - 2rb \cos \gamma \quad (4)$$

The term  $rb \cos \gamma$  is the dot product  $\bar{b} \cdot (\bar{r}_s - \bar{r}_g)$ .

$$rb \cos \gamma = \bar{b} \cdot (\bar{r}_s - \bar{r}_g) = x_b(x_s - x_g) + y_b(y_s - y_g) + z_b(z_s - z_g) \quad (5)$$

Equation 4 can now be solved for  $\ell$  by taking the square root and substituting Equation 5.

$$\ell = [r^2 + b^2 - 2\bar{b} \cdot (\bar{r}_s - \bar{r}_g)]^{1/2} - r \quad (6)$$

The parameters that are to be included in the solution are

$$x_b, y_b, z_b, \ell_1, \text{ and } \ell_2,$$

which represent the baseline vector and the receiver differences.

For each parameter, there is an initial estimate that is to be improved by using the observations. The computed value  $L_c$  is obtained from Equation 3, using the initial estimates. The observed value is  $L_o$ . These will differ by an amount  $\Delta L$  such that

$$L_o = L_c + \Delta L$$

The problem is linearized if  $L_c$  and  $\Delta L$  are taken to be the first and second terms of a Taylor's series expanded about the initial estimate. The third and higher terms are omitted. The expanded second term is

$$\Delta L = \frac{\partial L_c}{\partial x_b} \Delta x_b + \frac{\partial L_c}{\partial y_b} \Delta y_b + \frac{\partial L_c}{\partial z_b} \Delta z_b + \frac{\partial L_c}{\partial \ell_1} \Delta \ell_1 + \frac{\partial L_c}{\partial \ell_2} \Delta \ell_2 \quad (8)$$

The required partial derivatives are obtained from Equations 3 and 6:

$$\frac{\partial L_c}{\partial x_b} = [r^2 + b^2 - 2\bar{b} \cdot (\bar{r}_s - \bar{r}_g)]^{-\frac{1}{2}} (x_b - x_s + x_g)$$

$$\frac{\partial L_c}{\partial y_b} = [r^2 + b^2 - 2\bar{b} \cdot (\bar{r}_s - \bar{r}_g)]^{-\frac{1}{2}} (y_b - y_s + y_g)$$

(9)

$$\frac{\partial L_c}{\partial z_b} = [r^2 + b^2 - 2\bar{b} \cdot (\bar{r}_s - \bar{r}_g)]^{-\frac{1}{2}} (z_b - z_s + z_g)$$

$$\frac{\partial L_c}{\partial \ell_1} = 1$$

$$\frac{\partial L_c}{\partial \ell_2} = t_R - t_o$$

The system of equations represented by Equation 7 can be placed into matrix form and solved using weighted batch least squares. Each row represents one smoothed observation.

$$\begin{vmatrix} (L_o - L_c)_1 \\ (L_o - L_c)_2 \\ \vdots \\ \vdots \\ (L_o - L_c)_n \end{vmatrix} = \begin{vmatrix} \left( \frac{\partial L_c}{\partial x_b} \right)_1 & \left( \frac{\partial L_c}{\partial y_b} \right)_1 & \left( \frac{\partial L_c}{\partial z_b} \right)_1 & 1 & (t_{R1} - t_o) \\ \left( \frac{\partial L_c}{\partial x_b} \right)_2 & \left( \frac{\partial L_c}{\partial y_b} \right)_2 & \left( \frac{\partial L_c}{\partial z_b} \right)_2 & 1 & (t_{R2} - t_o) \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ \left( \frac{\partial L_c}{\partial x_b} \right)_n & \left( \frac{\partial L_c}{\partial y_b} \right)_n & \left( \frac{\partial L_c}{\partial z_b} \right)_n & 1 & (t_{Rn} - t_o) \end{vmatrix} \begin{vmatrix} \Delta x_b \\ \Delta y_b \\ \Delta z_b \\ \Delta \ell_1 \\ \Delta \ell_2 \end{vmatrix} \quad (10)$$

The matrix of partials is denoted by A, and the parameters to be improved are denoted by X. The above then reduces to the form

$$L_o - L_c = AX$$

Then,

$$A^T W A X = A^T W (L_o - L_c)$$

and

$$X = (A^T W A)^{-1} A^T W (L_o - L_c)$$

The matrix  $(A^T W A)^{-1}$  is the covariance matrix.

The diagonal weight matrix  $W$  is introduced to give smoothed observations with low noise more weight in the solution than those with high noise. The relative weights are obtained from the RSS of the RMS computed from the two smoothing polynomials that comprise the particular observation.

The solution vector  $X$  is then added to the initial estimate of

$$x_b, y_b, z_b, \ell_1, \text{ and } \ell_2$$

to obtain the improved values. The standard deviation in this result is obtained from the square root of the diagonals of the covariance matrix. The confidence that one places in these standard deviations depends upon how well the fluctuations in the observations agree with the statistical assumptions inherent in the least-squares process. Unmodeled effects (e.g., systematic errors in  $\bar{r}_s$  or variable instrumental biases) can lead to solutions whose true error is much larger than the computed standard deviation. When unmodeled effects are known to be present in the data, the standard deviations can only be viewed as a guide indicating the geometric strength of the observations and subsequent solution.

## OBSERVATIONS

January 1981, both NGRS-1 and NGRS-2 were operated side by side at NSWC. Pseudorange and Doppler data were recorded in the usual manner while the receivers simultaneously observed the same GPS satellites. Two antenna sites were in use: a surveyed site and a site approximately 2 m south. The receivers spent time connected to a common antenna and to their individual antenna. Also, a common frequency standard was used, as well as individual frequency standards. Table 2 lists the number of 20-min segments obtained from each satellite on each day. For each segment, a residual difference in range is computed.. The mean and standard deviations of these residuals for all segments on a given day are presented. The significance of these residuals is discussed in the next section.

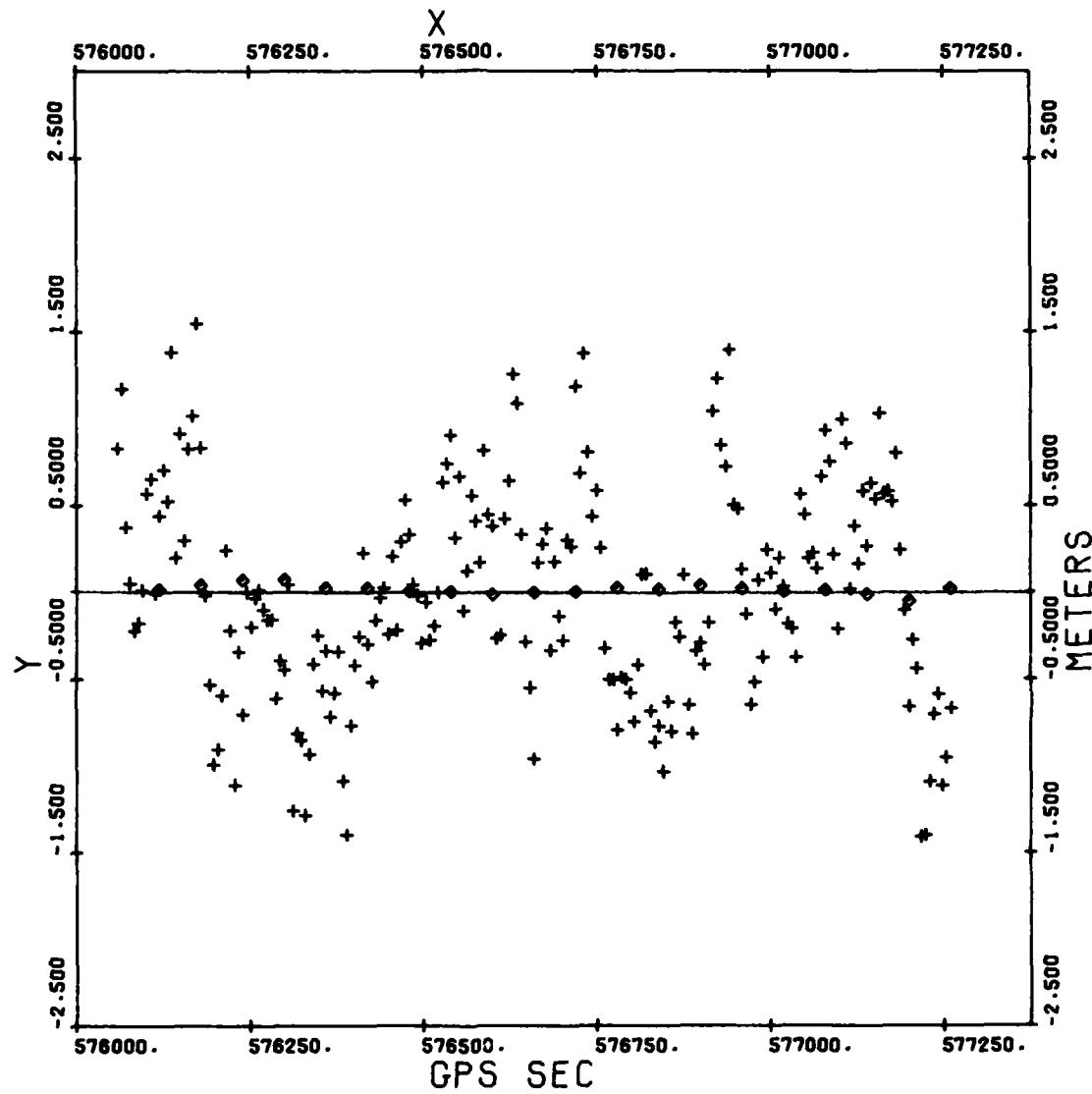
**Table 2. Segment Statistics For Each Days Observations**

Day (January 1981)	10	12	15	16	17	18	19
Antenna	Common		Separate		Common Separate		
Frequency Standard	Common		Common				
<b>SV-5</b>							
Number of Segments	23	32	25	22	27	28	14
Mean (m)	0.129	0.138	0.207	0.208	0.112	0.116	0.107
Standard Deviation (m)	0.019	0.026	0.038	0.032	0.021	0.024	0.014
<b>SV-6</b>							
Number of Segments	14	8	11	14	14	14	13
Mean (m)	0.110	0.114	0.218	0.221	0.086	0.091	0.095
Standard Deviation (m)	0.009	0.018	0.025	0.042	0.018	0.011	0.015
<b>SV-8</b>							
Number of Segments	10	0	8	12	15	15	16
Mean (m)	0.109		0.188	0.220	0.090	0.090	0.094
Standard Deviation (m)	0.013		0.007	0.025	0.024	0.019	0.012
<b>SV-9</b>							
Number of Segments	18	18	17	7	18	16	5
Mean (m)	0.158	0.154	0.212	0.265	0.133	0.144	0.149
Standard Deviation (m)	0.038	0.032	0.025	0.062	0.031	0.027	0.031

### NOISE PROBLEM

Unfortunately, a problem with the 5010 receiver in NGRS-2 caused the pseudorange observations to have a higher noise level than comparable observations obtained from NGRS-1. This fault, which was later identified and corrected, degraded the NGRS-2 pseudorange data somewhat. The nature of the degradation is illustrated by the Figures 2 through 5.

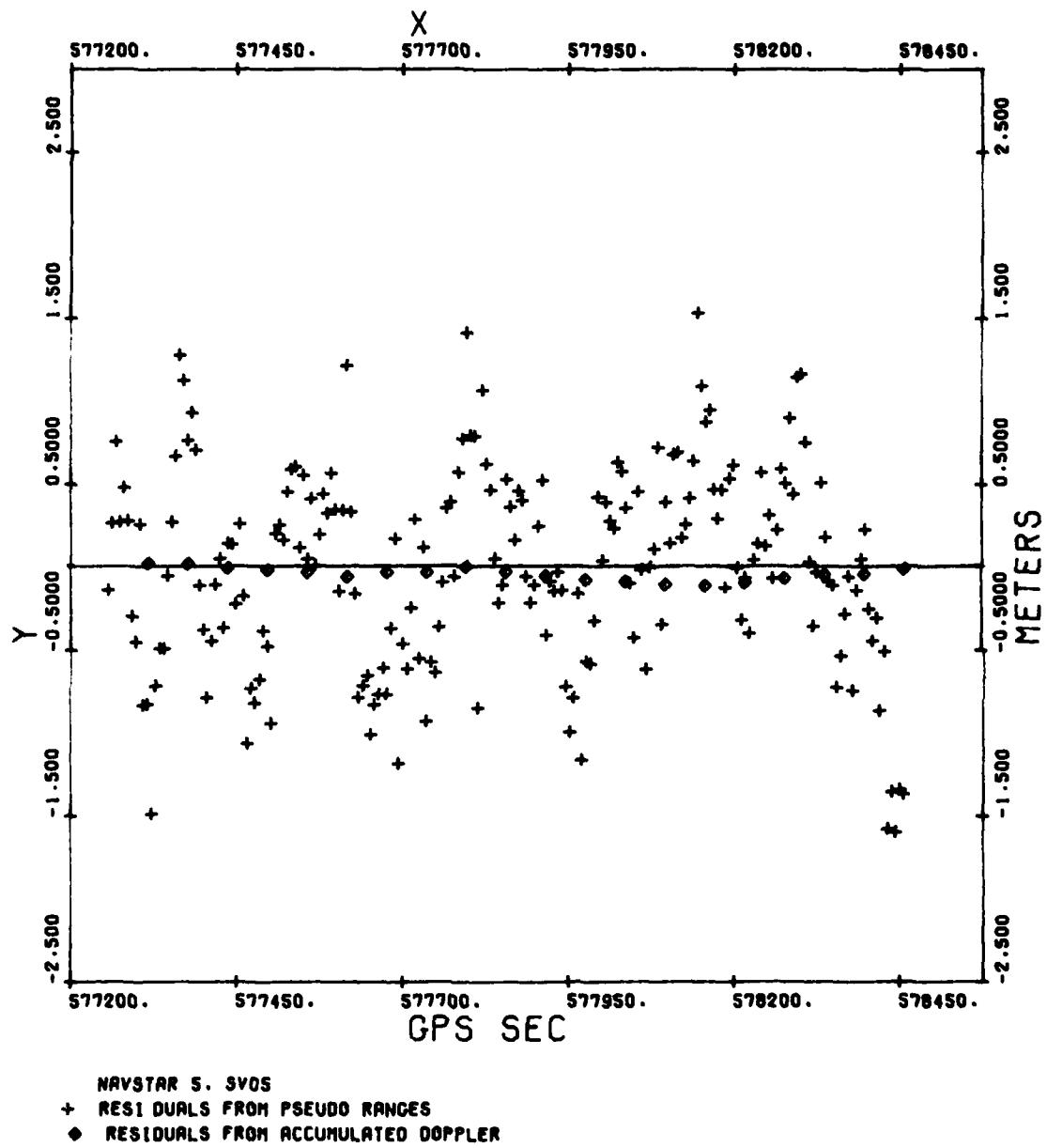
Twenty-min segments of data were fit by a fourth-degree polynomial, as previously described. Both  $L_1$  6-s pseudoranges and  $L_1$  60-s integrated Doppler range differences contributed to the fit. Figure 2 shows plots of the fit residuals of two consecutive 20-min segments of data from NGRS-1. Figure 3 shows similar residuals over the same span from NGRS-2. The diamond symbols represent range difference residuals from Doppler, added consecutively to produce a biased range. For plotting purposes, the bias was supplied by evaluating the polynomial at the time of the beginning



NAVSTAR S. SV05  
 + RESIDUALS FROM PSEUDO RANGES  
 ◇ RESIDUALS FROM ACCUMULATED DOPPLER

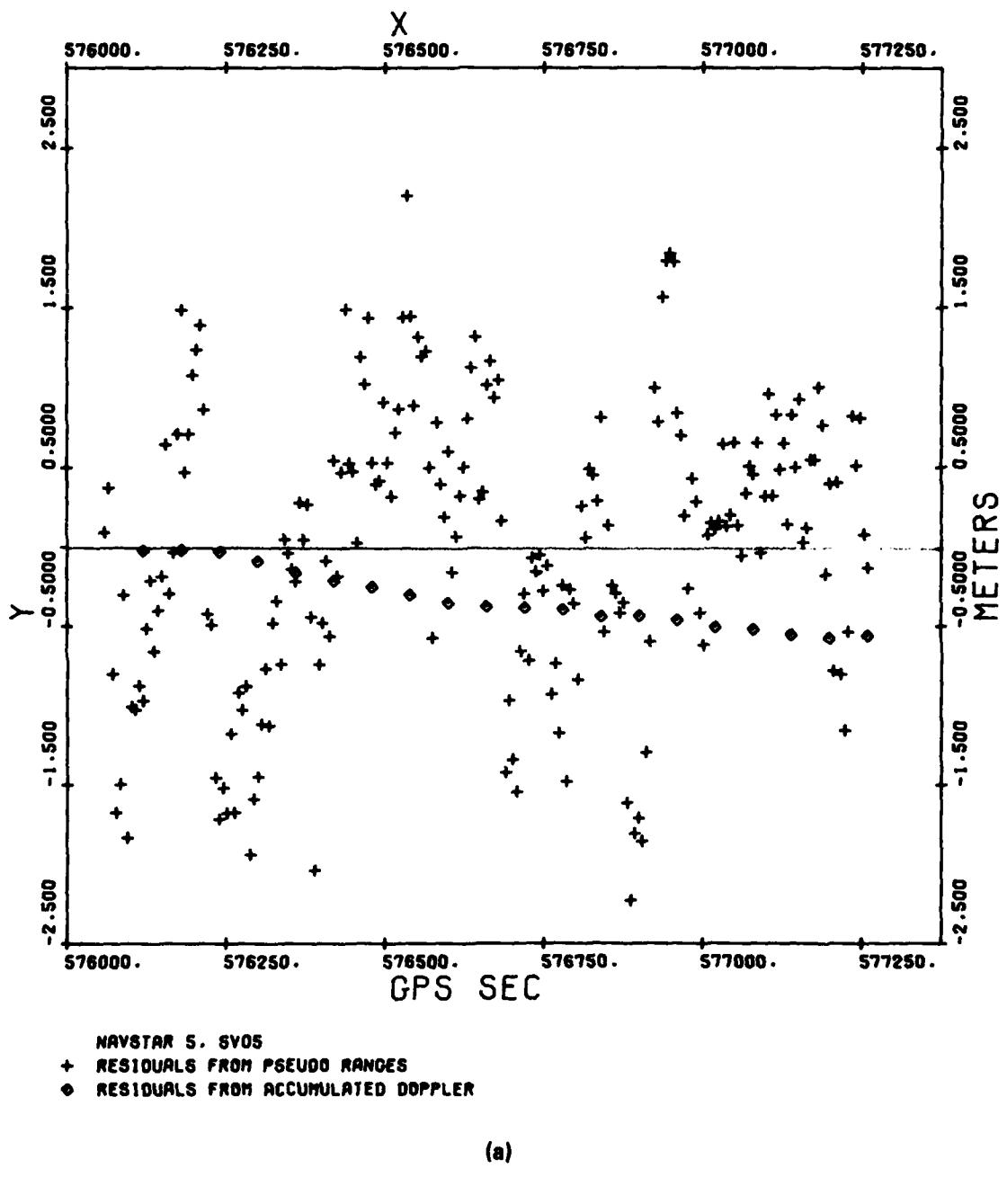
(a)

Figure 2. NGRS-1 Residuals From 20-Min Smoothing Polynomial,  
 NSWC/Dahlgren, Day 10, 1981

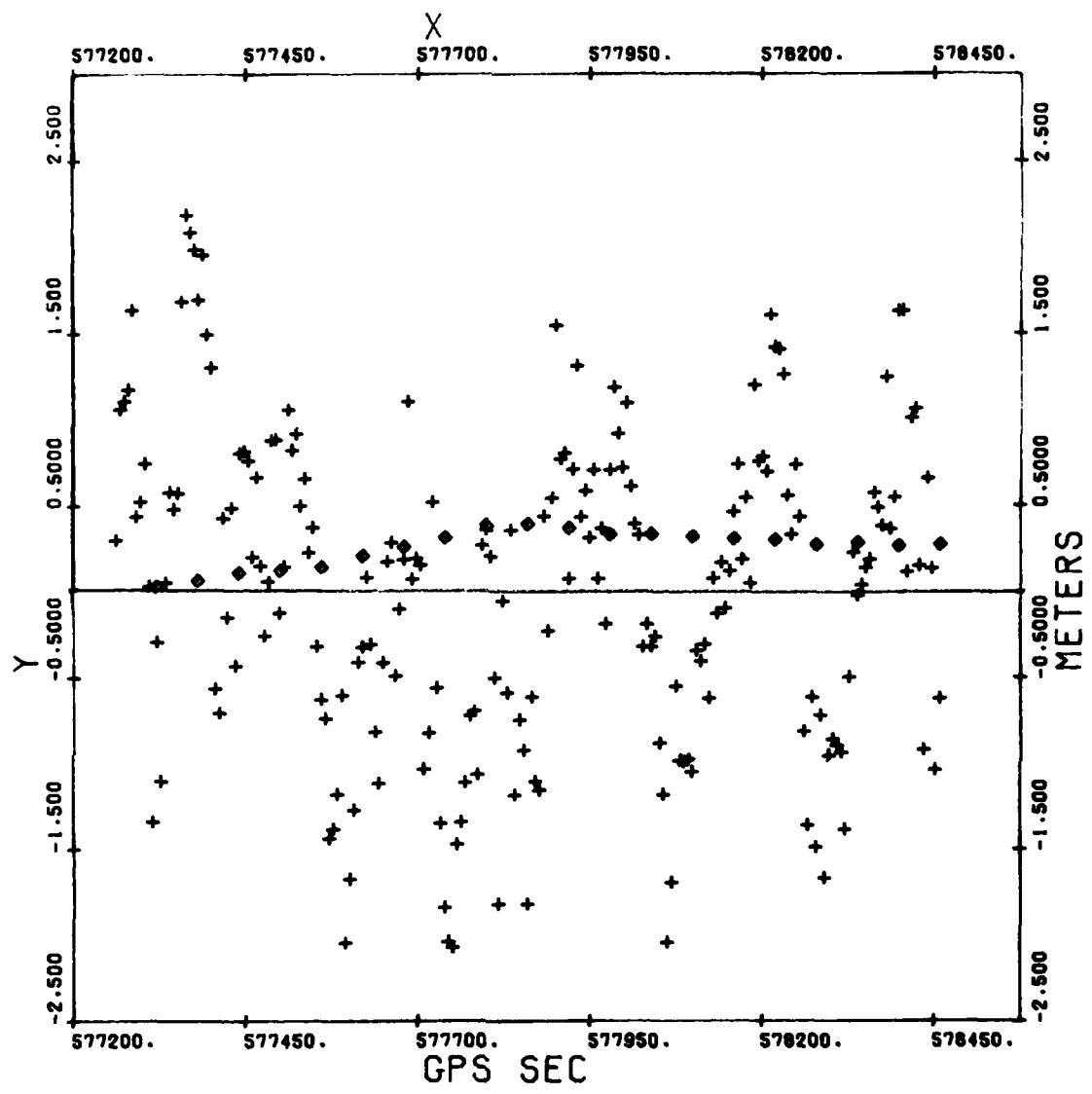


(b)

Figure 2. NGRS-1 Residuals From 20-Min Smoothing Polynomial,  
NSWC/Dahlgren, Day 10, 1981 (Continued)

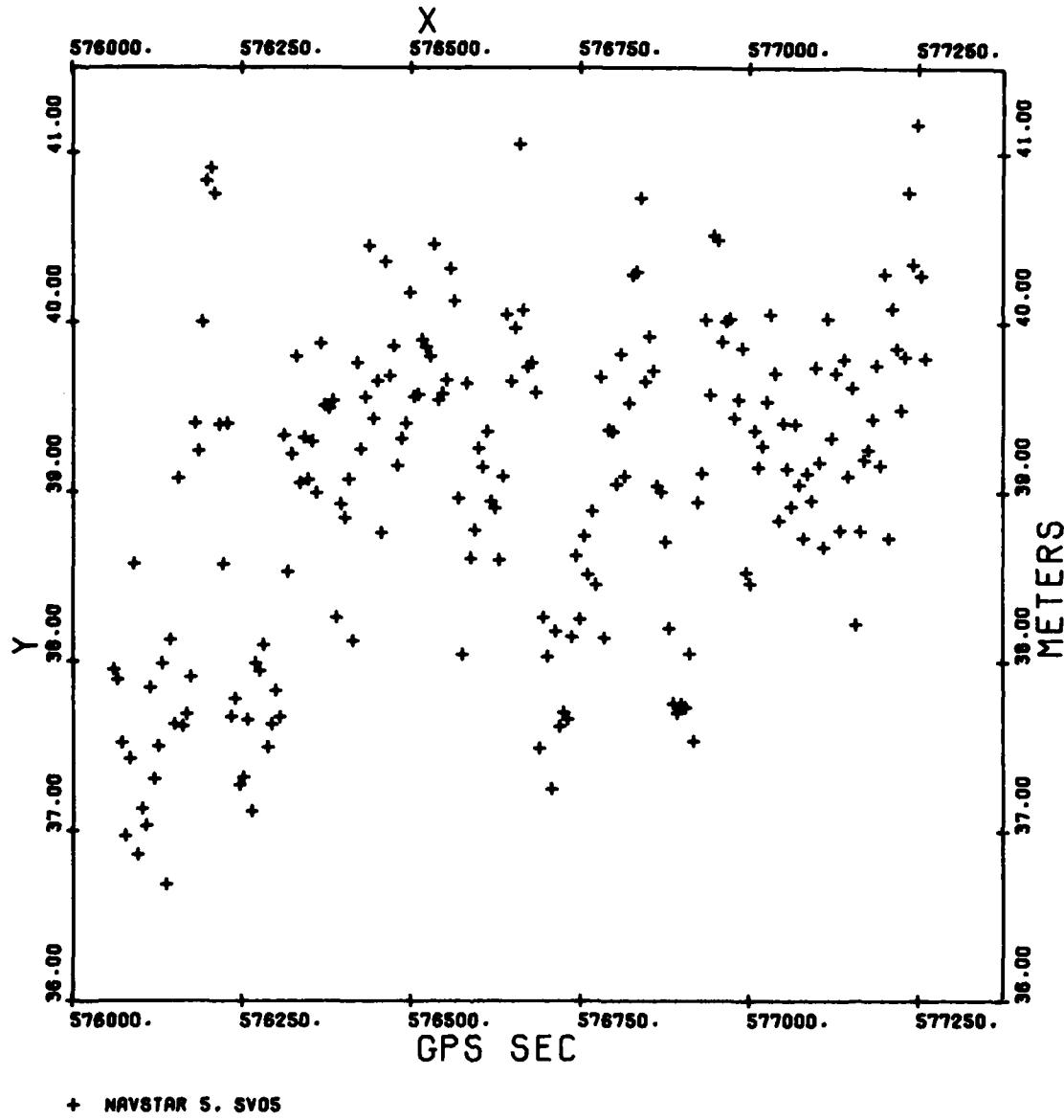


**Figure 3. NGRS-2 Residuals From 20-Min Smoothing Polynomial,  
NSWC/Dahlgren, Day 10, 1981**



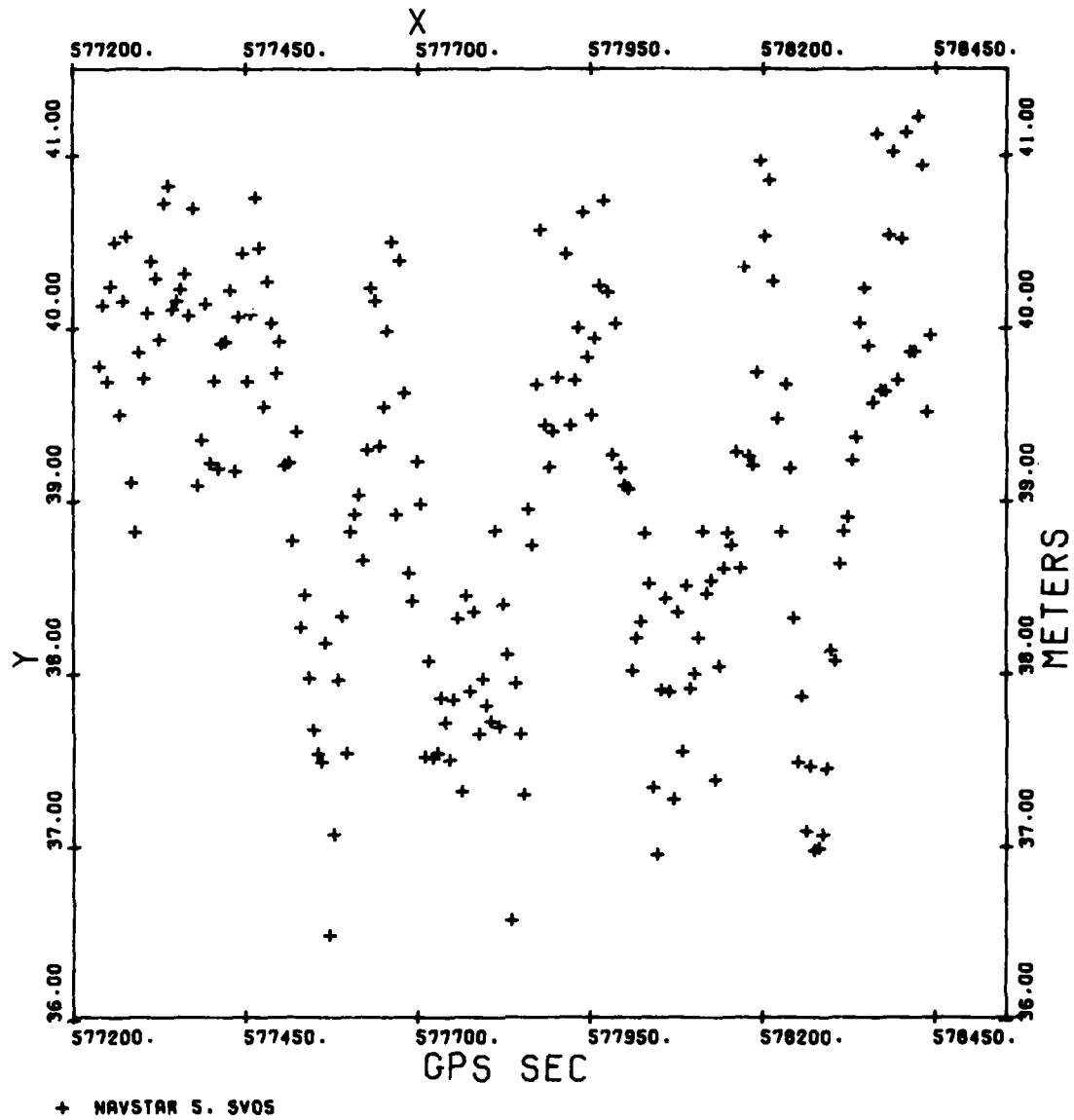
(b)

**Figure 3. NGRS-2 Residuals From 20-Min Smoothing Polynomial,  
NSWC/Dahlgren, Day 10, 1981 (Continued)**



(a)

**Figure 4. Differences in Pseudorange (20-Min), NGRS-2-NGRS-1,  
NSWC/Dahlgren, Day 10, 1981**



(b)

**Figure 4. Differences in Pseudorange (20-Min), NGRS-2-NGRS-1, NSWC/Dahlgren, Day 10, 1981 (Continued)**

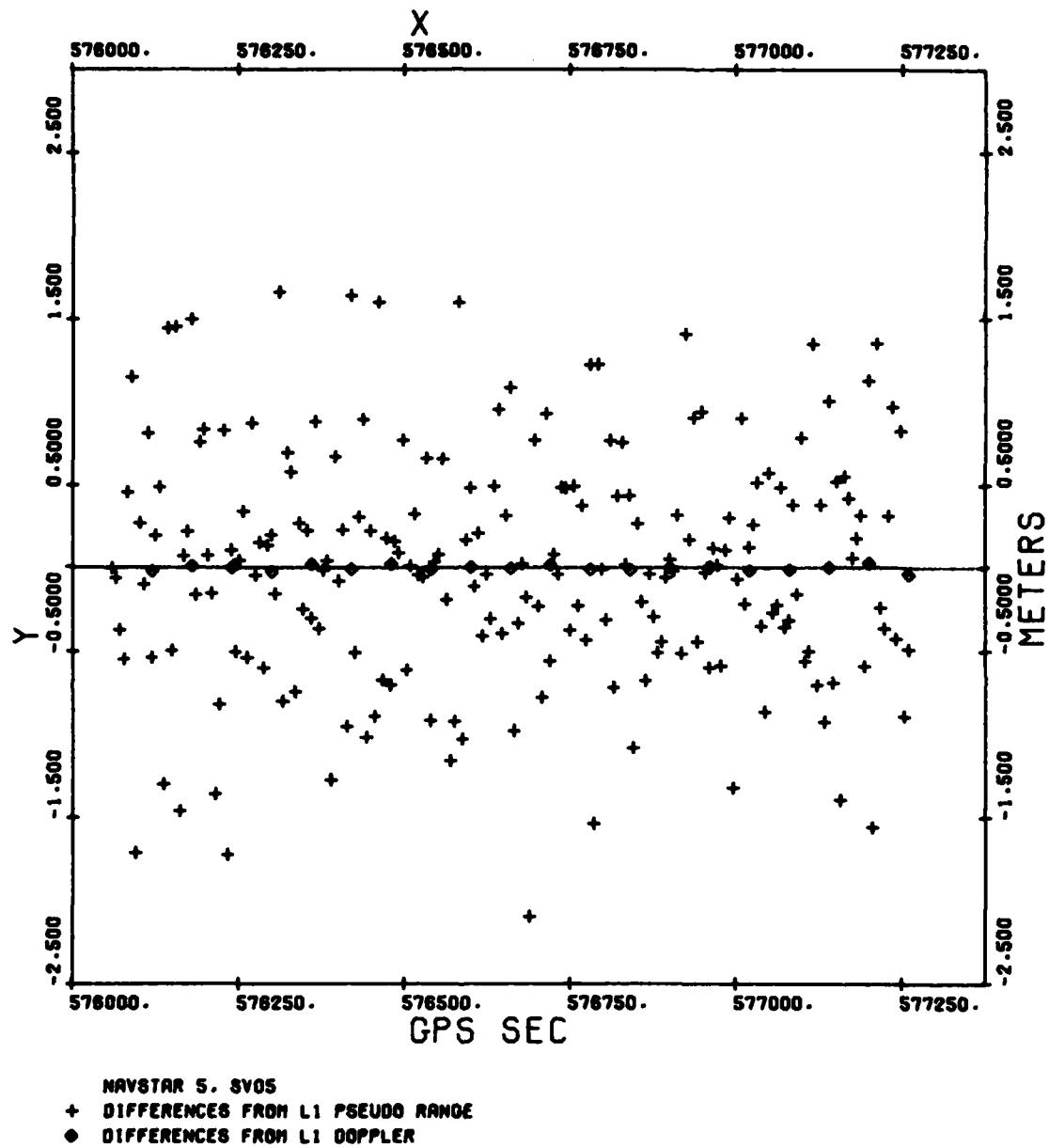
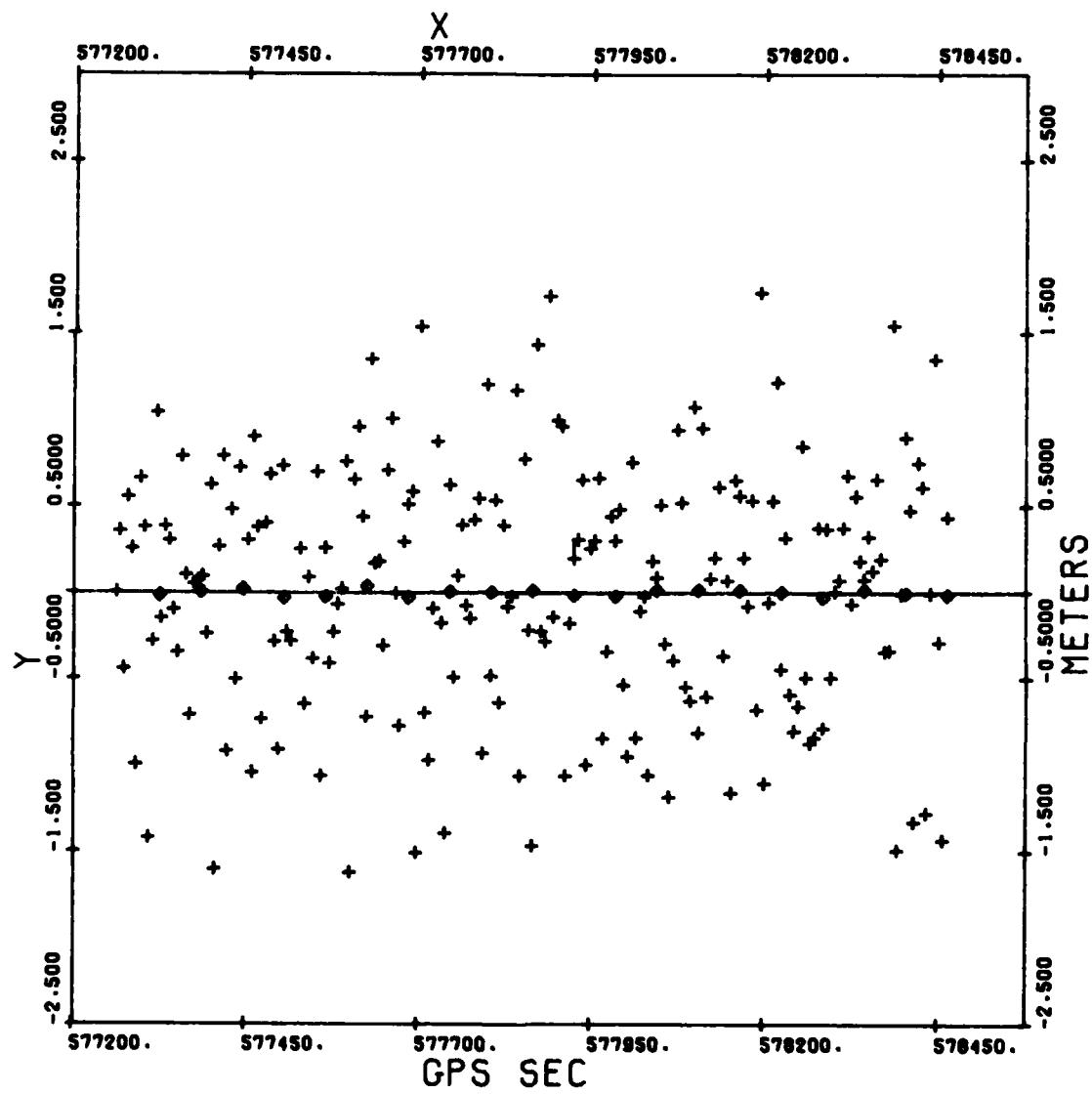


Figure 5. Differences in Range Differences, NGRS-2-NGRS-1,  
NSWC/Dahlgren, Day 10, 1981



(b)

**Figure 5. Differences in Range Differences, NGRS-2-NGRS-1,  
NSWC/Dahlgren, Day 10, 1981 (Continued)**

of the first Doppler observation. The plus symbols are the pseudorange residuals. In the case of NGRS-1, the biased ranges and pseudorange are consistent, since the residuals are centered about zero. In the case of NGRS-2, the consistency is not as good.

In Figure 3(a) the biased range residuals deviate below the zero axis; and in Figure 3(b), they deviate above the axis. The problem appears to be a random short-term drift in the NGRS-2 pseudoranges. Evidence for this has been gathered by plotting the differences of the pseudoranges obtained from the two receivers. The differences should be constant over the interval, because both receivers were connected to the same antenna and both were being driven by the same frequency standard. The difference plots (Figures 4) show several meters of scatter and a tilt with positive slope (Figure 4a) and negative slope (Figure 4b). The differences in range differences between the two receivers (Figure 5) show no similar trends; thus, the fault appears to lie with the pseudorange bias from NGRS-2. The computed RMS for all these residual plots is listed in Table 3.

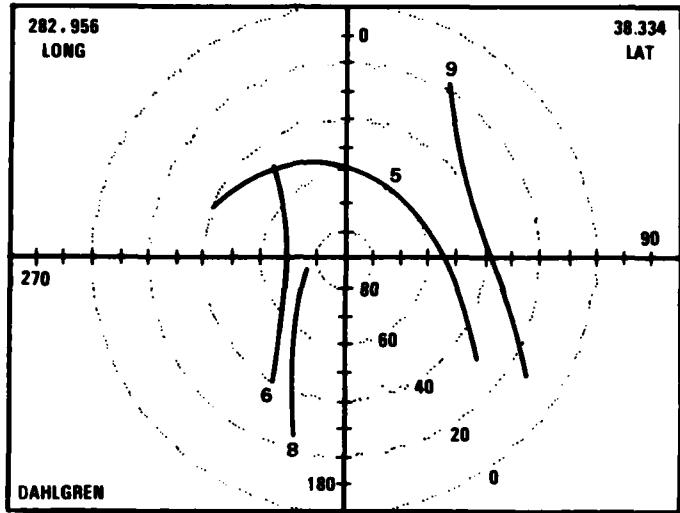
**Table 3. RMS of Residual Plots**

	<u>Figure</u>	<u>NGRS</u>	<u>SPAN</u>	<u>RMS (m)</u>
Smoothing Polynomials	2a	1	1	0.59
	2b	1	2	0.57
	3a	2	1	0.85
	3b	2	2	0.88
Pseudorange Differences	4a	2-1	1	0.95
	4b	2-1	2	1.09
Differences of Range Differences	5a	2-1	1	0.68
	5b	2-1	2	0.68

## SOLUTIONS

### DAYS 10 AND 12

Data from the two days in which the receivers used common antennas and common frequency standards have been processed in the manner described in the previous sections. Figure 6 shows the segments of the satellite ground tracks observed on day 10. The tracks for day 12 were similar, except that the observations of SV-8 were omitted.



**Figure 6. Azimuth and Elevation Tracks of Satellites From Site on Day 10**

All observations were smoothed over a period of 10 min; therefore, they consist of 100 pseudoranges and 10 range differences. The number of 10-min segments available on each day is listed in Table 2. The baseline vector  $\bar{b}$  was purposely offset by 4 m in each-earth fixed component in these solutions in order to demonstrate that the data produces corrections to  $\bar{b}$  in the correct direction. These corrections should be -4 m in each component. The results obtained are summarized in Table 4. A second solution was performed in which the parameter  $\ell_2$  was constrained, by a priori sigmas, to zero. This procedure improved the result on day 10, but worsened the result on day 12. Table 5 presents this solution.

An additional experiment using just six 10-min segments was performed. These segments (Table 6) were selected so that they were spread in azimuth around the site and were nearly the same on day 12 as on day 10. Observations from SV-8 were omitted from both. The solutions obtained are quite reasonable (Table 7) and illustrate the importance of choosing observations that cover the site from all sides. Similar solutions using data from just one satellite (SV-6, SV-8, or SV-9) were poor due to the absence of data from two or more quadrants.

## **DAYS 15 AND 16**

Data from the two days in which the receivers used common frequency standards but separate antennas were processed; the baseline was to be assumed zero. In fact, the antenna for NGRS-2 was placed 2 m south and 0.2 m east of the NGRS-1 antenna. On day 15, the satellites observed were SV-5, 6, and 9; on day 16, SV-5, 6, and 8 were observed. A solution using these data is presented in Table 8. Separate solutions using only the data from each day are given in Table 9. All of these solutions are rotated from earth-fixed components to a local vertical frame with components that are labeled North, East, and Vertical, so that comparison with the known baseline is possible.

Even though the standard deviations indicate that the vertical component is the best-determined of the three components, it contributes the largest error. The excessive receiver noise during these two days (as noted in Table 2) may have been a contributing factor to the poor results obtained in this component.

## **DAYS 17, 18, AND 19**

During the last three days of this experiment, the two systems operated from independent frequency standards, but utilized a common antenna. The solutions obtained were comparable with those on days 10 and 12, when a common frequency standard was used. The values for the bias  $\ell_1$  and drift  $\ell_2$  are larger than they had previously been because of the addition of the relative epoch offset that exists between the two frequency standards.

A combined solution using all the data collected during these three days (a total of 195 10-min segments) is presented in Table 10. Again, a 4-m offset in each component was introduced. Separate solutions for days 18 and 19 were also made (Table 11). Though the standard deviations are smaller in the three-day solution, the magnitude of the error is greater than that found in the single-day solutions. This result tends to indicate that the bias model fits the data better over a short time span. A result similar to this has been predicted by Fell<sup>4</sup>.

**Table 4. Solutions Using All Available Data, Days 10 and 12**

<u>Day</u>	<u>Component</u>	<u>Solution</u>	<u>Sigma</u>	<u>Solution - True</u>	<u>Units</u>
10	x	-3.570	0.052	0.430	m
	y	-5.171	0.109	-1.171	m
	z	-3.448	0.090	0.552	m
	$\ell_1$	38.580	0.093	—	m
	$\ell_2$	$17.658 \times 10^{-6}$	$0.996 \times 10^{-6}$	—	m/s
12	x	-3.955	0.060	0.045	m
	y	-4.432	0.130	-0.432	m
	z	-3.830	0.101	0.170	m
	$\ell_1$	38.499	0.105	—	m
	$\ell_2$	$-1.714 \times 10^{-6}$	$0.935 \times 10^{-6}$	—	m/s
				<u>Day 10</u>	<u>Day 12</u>
Magnitude (Solution - True)				1.364	0.466

**Table 5. Solutions Using All Available Data, Parameter  $\ell_2$  Constrained, Days 10 and 12**

<u>Day</u>	<u>Component</u>	<u>Solution</u>	<u>Sigma</u>	<u>Solution - True</u>	<u>Units</u>
10	x	-3.543	0.052	0.457	m
	y	-4.181	0.094	-0.181	m
	z	-4.279	0.076	-0.279	m
	$\ell_1$	38.419	0.093	—	m
	$\ell_2$	0.0	0.0	—	m
12	x	-3.978	0.059	0.022	m
	y	-4.555	0.112	-0.555	m
	z	-3.719	0.080	0.281	m
	$\ell_1$	38.540	0.103	—	m
	$\ell_2$	0.0	0.0	—	m
				<u>Day 10</u>	<u>Day 12</u>
Magnitude (Solution - True)				0.565	0.622

**Table 6. Azimuth And Elevation of Six Segments Selected From Days 10 and 12**

	Azimuth (Degrees)		Elevation (Degrees)	
	<u>Day 10</u>	<u>Day 12</u>	<u>Day 10</u>	<u>Day 12</u>
SV-5	310.8	313.5	46.2	47.0
	116.9	115.9	40.1	40.8
SV-6	230.4	226.5	61.6	59.4
	211.5	210.6	42.6	41.0
SV-9	85.4	85.4	39.0	39.1
	33.9	33.9	21.9	21.9

**Table 7. Solutions Using Six Selected Segments, Days 10 and 12**

<u>Day</u>	<u>Component</u>	<u>Solution</u>	<u>Sigma</u>	<u>Solution - True</u>	<u>Units</u>
10	x	-3.805	0.197	-0.195	m
	y	-3.768	0.380	-0.232	m
	z	-4.552	0.376	0.552	m
	$\ell_1$	37.356	0.361	—	m
	$\ell_2$	$18.736 \times 10^{-6}$	$3.426 \times 10^{-6}$	—	m/s
12	x	-3.557	0.622	-0.443	m
	y	-5.052	0.373	1.052	m
	z	-3.192	0.414	-0.808	m
	$\ell_1$	39.264	0.557	—	m
	$\ell_2$	$-5.178 \times 10^{-6}$	$10.559 \times 10^{-6}$	—	m/s
			<u>Day 10</u>	<u>Day 12</u>	
<b>Magnitude (Solution - True)</b>			0.630	1.399	

**Table 8. Combined Solution Using All Available Data, Days 15 and 16**

<u>Day</u>	<u>Component</u>	<u>Solution</u>	<u>Sigma</u>	<u>Solution - True</u>	<u>Units</u>
15 and 16	North	-2.122	0.157	-.122	m
	East	0.553	0.100	.353	m
	Vertical	-1.353	0.035	-1.653	m
	$\ell_1$	49.276	0.133	—	m
	$\ell_2$	$-1.104 \times 10^{-6}$	$0.557 \times 10^{-6}$	—	m/s

Days 15 and 16

Magnitude (Solution - True) 1.695

**Table 9. Separate Solutions, Days 15 and 16**

<u>Day</u>	<u>Component</u>	<u>Solution*</u>	<u>Sigma</u>	<u>Solution - True</u>	<u>Units</u>
15	North	-2.672	0.507	-.672	m
	East	-0.018	0.233	-.220	m
	Vertical	1.200	0.232	1.200	m
	$\ell_1$	50.228	0.185	—	m
	$\ell_2$	$-38.980 \times 10^{-6}$	$12.878 \times 10^{-6}$	—	m/s
16	North	-1.844	0.307	0.156	m
	East	0.869	0.178	0.669	m
	Vertical	-3.727	0.104	-3.727	m
	$\ell_1$	47.254	0.538	—	m
	$\ell_2$	$0.366 \times 10^{-6}$	$6.396 \times 10^{-6}$	—	m/s

Day 15

Day 16

Magnitude (Solution - True) 1.393 m 3.790 m

\*Day 15: SV-5, 6, 9  
Day 16: SV-5, 6, 8

**Table 10. Combined Solution Using All Available Data, Days 17, 18, and 19**

<u>Day</u>	<u>Component</u>	<u>Solution</u>	<u>Sigma</u>	<u>Solution - True</u>	<u>Units</u>
17, 18, and 19	x	-4.512	0.030	-0.512	m
	y	-5.548	0.047	-1.548	m
	z	-3.327	0.032	0.673	m
	$\ell_1$	-3177.808	0.046	—	m
	$\ell_2$	$-136.653 \times 10^{-6}$	$0.102 \times 10^{-6}$	—	m/s

Days 17, 18 and 19

Magnitude (Solution - True) 1.764 m

**Table 11. Separate Daily Solutions, Days 18 and 19**

<u>Day</u>	<u>Component</u>	<u>Solution</u>	<u>Sigma</u>	<u>Solution - True</u>	<u>Units</u>
18	x	-4.869	0.052	-0.869	m
	y	-4.432	0.114	-0.432	m
	z	-4.029	0.057	-0.312	m
	$\ell_1$	-3179.838	0.202	—	m
	$\ell_2$	$-118.217 \times 10^{-6}$	$2.206 \times 10^{-6}$	—	m/s
19	x	-3.887	0.058	0.133	m
	y	-5.402	0.124	-1.402	m
	z	-3.762	0.062	0.238	m
	$\ell_1$	-3184.151	0.408	—	m
	$\ell_2$	$-96.008 \times 10^{-6}$	$2.334 \times 10^{-6}$	—	m/s

Day 18      Day 19

Magnitude (Solution - True) 1.303 m      1.427 m

## CONCLUSIONS

Relative positioning on a short baseline using single-frequency pseudoranges and range differences from Doppler is permissible if the mission accuracy requirements are set at 2-m or greater. The time on site need not be great if enough satellites are in view to satisfy the geometric requirements of the desired solution. This is demonstrated by the data in Table 6, for which only 1 hr (six 10-min segments) of observations were used to produce a solution with errors comparable to those obtained from 10 times as much data.

The standard deviations in all cases were highly optimistic when compared with the actual errors obtained. This indicates that the RMS of the residuals to each segment is not representative of the true errors involved. There appears to be something akin to time-variable channel biases operating that cannot be absorbed by the  $\ell_1$  and  $\ell_2$  parameters. Some method for on-line calibration, using locally generated stable test signals, is needed in order to derive corrections for this interchannel bias fluctuation.

Other methods of treating these data are capable of producing better results. In particular, relative positioning using the Doppler data alone allows a more precise solution to be obtained. Figures 2 and 3 can be used to indicate the superior quality of the accumulated Doppler vs the pseudoranges for this data set. Processing of this same data span using Doppler only has been reported elsewhere.<sup>5</sup>

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